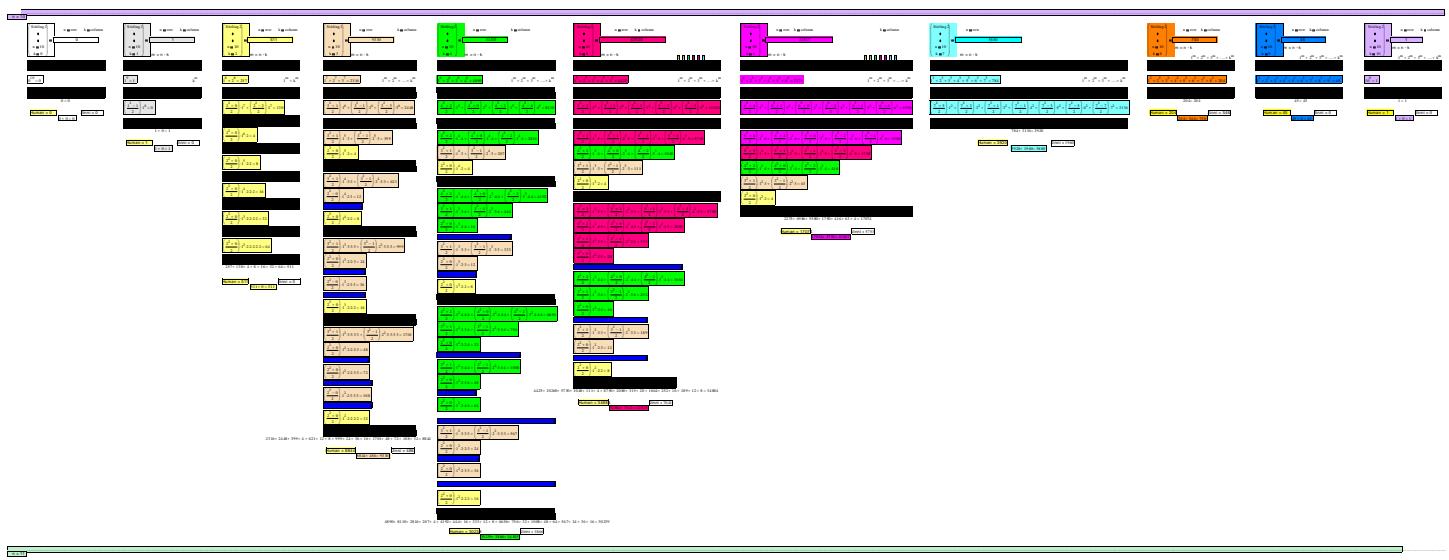


Stirling numbers of the second kind table

Algorithm family tree of the Human and Jinni

Serajian Asl





Below is a sample of a Human term in Human's equation:

Base numbers in numerator {variable}

Generation Grade, {variable} for changing the generation

Coefficients between the first and the last coefficients {variable}

$$\left(\frac{6^2 + 2}{2}\right) * \color{magenta}{3^8} * \color{yellow}{4} * \color{yellow}{4} * \color{yellow}{5} * \color{cyan}{5}$$

First coefficient (invariable)

First coefficient (invariable)

Last coefficient as identity of equation (invariable)

Below is a sample of Human's sons set:

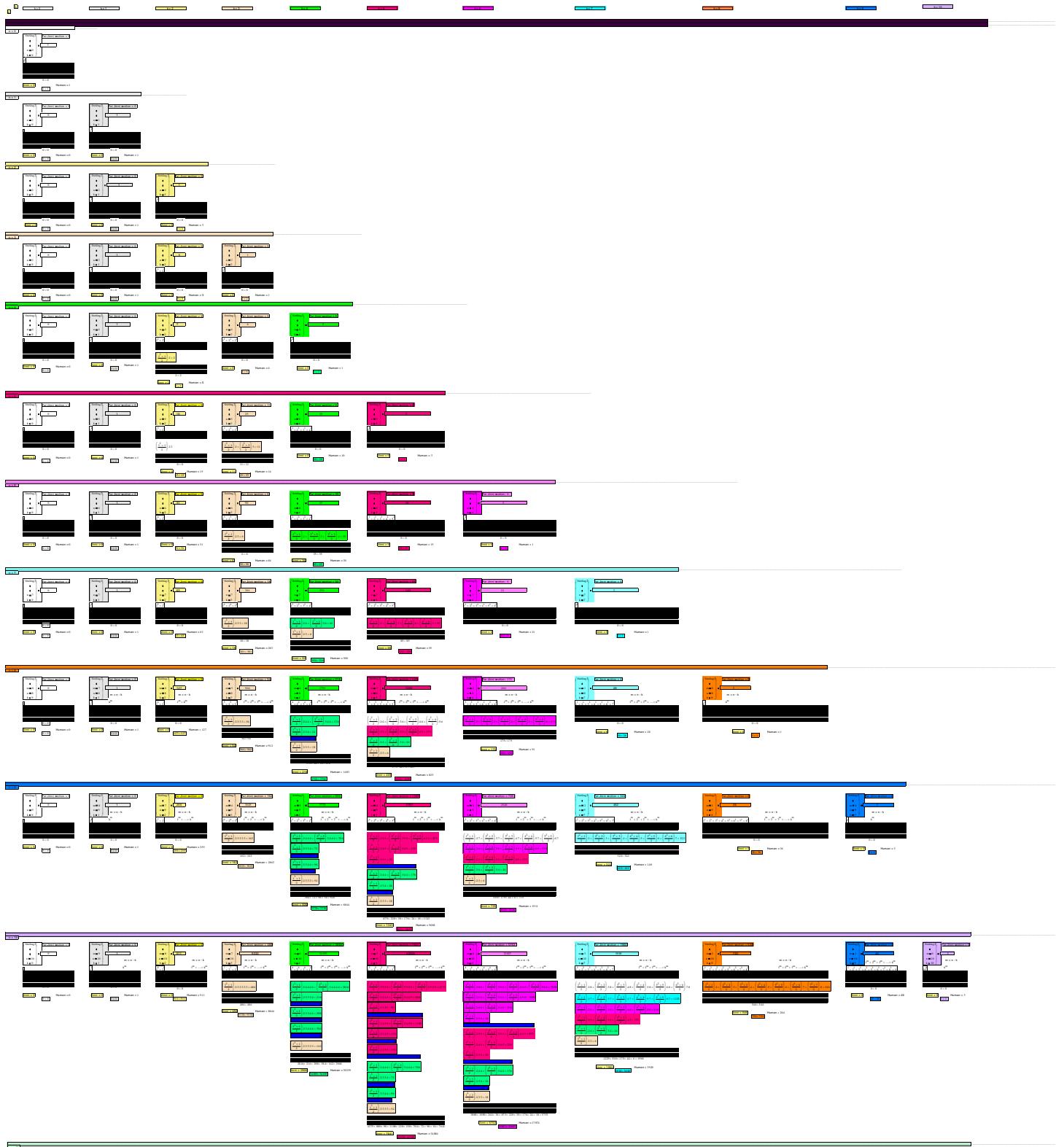
$$\left(\frac{3^2+1}{2}\right) * \textcolor{red}{1^4} * \textcolor{blue}{3} * \textcolor{red}{3} + \left(\frac{3^2-1}{2}\right) * \textcolor{red}{2^4} * \textcolor{blue}{3} * \textcolor{red}{3} = 621$$

$$\left(\frac{2^2 - 0}{2}\right) * 1^4 * 2 * 3 = 12$$

Stirling numbers of the second kind triangular **set of equation packages** array

Basis on family tree of the **Jinni** and Human algorithm

Serajian Asl



Below is a sample of a Jinni term in jinni's equation:

Base numbers in numerator {invariable}

$$\left(\frac{3^2+3}{2}\right) * 4 * 5 * 5 * 5 * 5$$

Coefficients between the first and the last coefficients {variable}

First coefficient (invariable)

Last coefficient as identity of equation (invariable)

Below is a sample of Jinni's sons set:

$$\left(\frac{1^2+1}{2}\right) * 2 * 5 * 5 * 5 + \left(\frac{2^2+2}{2}\right) * 3 * 5 * 5 * 5 + \left(\frac{3^2+3}{2}\right) * 4 * 5 * 5 * 5 = 4375$$

$$\left(\frac{1^2+1}{2}\right) * 2 * 4 * 4 * 5 + \left(\frac{2^2+2}{2}\right) * 3 * 4 * 4 * 5 = 880$$

$$\left(\frac{1^2+1}{2}\right) * 2 * 3 * 3 * 5 = 90$$

Generalized stirling numbers

Magic Cube basis on Stirling numbers (Serajian Asl)

"Figure 1"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1							
2	1	1						
3	1	3	1					
4	1	7	6	1				
5	1	15	25	10	1			
6	1	31	90	65	15	1		
7	1	63	301	350	140	21	1	
8	1	127	966	1701	1050	266	28	1
9	1	255	3025	7770	6951	2646	462	36
10	1							

By transferring the Stirling triangular array's columns to top of the array, we will have a **squared Array** named "**Stirling numerical squared array**"

"Figure 2"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	1	1	1	1	1	1	1
2	1	3	6	10	15	21	28	36
3	1	7	25	65	140	266	462	750
4	1	15	90	350	1050	2646	5880	11880
5	1	31	301	1701	6951	22827	63987	159027
6	1	63	966	7770	42525	179487	627396	1899612
7	1	127	3025	34105	246730	1323652	5715424	20912320
8	1	255	9330	145750	1379400	9321312	49329280	216627840
9	1							

Each one of the Stirling numbers that locates in rows of **Stirling numerical squared array**, is Equal with a **math relation**

For example series of the numbers which locates in row $n=3$ of Stirling numerical squared array is as below

$$\{1, 7, 25, 65, 140, 266, \dots, 1155, \dots\}$$

And each one of the numbers in above series is equal with a equation

"Figure 3"

$$\dots 1 = 1 \cdot \left(\frac{1^3 + 1^2}{2} \right)$$

$$\dots 7 = 1 \cdot \left(\frac{1^3 + 1^2}{2} \right) + 1 \cdot \left(\frac{2^3 + 2^2}{2} \right)$$

$$\dots 25 = 1 \cdot \left(\frac{1^3 + 1^2}{2} \right) + 1 \cdot \left(\frac{2^3 + 2^2}{2} \right) + 1 \cdot \left(\frac{3^3 + 3^2}{2} \right)$$

$$\dots 65 = 1 \cdot \left(\frac{1^3 + 1^2}{2} \right) + 1 \cdot \left(\frac{2^3 + 2^2}{2} \right) + 1 \cdot \left(\frac{3^3 + 3^2}{2} \right) + 1 \cdot \left(\frac{4^3 + 4^2}{2} \right)$$

$$140 = 1 \cdot \left(\frac{1^3 + 1^2}{2} \right) + 1 \cdot \left(\frac{2^3 + 2^2}{2} \right) + 1 \cdot \left(\frac{3^3 + 3^2}{2} \right) + 1 \cdot \left(\frac{4^3 + 4^2}{2} \right) + 1 \cdot \left(\frac{5^3 + 5^2}{2} \right)$$

$$266 = 1 \cdot \left(\frac{1^3 + 1^2}{2} \right) + 1 \cdot \left(\frac{2^3 + 2^2}{2} \right) + 1 \cdot \left(\frac{3^3 + 3^2}{2} \right) + 1 \cdot \left(\frac{4^3 + 4^2}{2} \right) + 1 \cdot \left(\frac{5^3 + 5^2}{2} \right) + 1 \cdot \left(\frac{6^3 + 6^2}{2} \right)$$

The set of **parenthesis's coefficients** in up relations make a triangular array as below

"Figure 4"

1									
1	1								
1	1	1							
1	1	1	1						
1	1	1	1	1					
1	1	1	1	1	1				
1	1	1	1	1	1	1			
1	1	1	1	1	1	1	1		

The other example, is set of numbers which locates in row $n = 4$ of Stirling numerical squared array.

$$\{1, 15, 90, 350, 1050, 2646, \dots, 5880\}$$

And each one of the numbers in above series is equal with a math relation

"Figure 5"

$$\dots 1 = \dots 1 \cdot \left(\frac{1^3 + 1^2}{2} \right)$$

$$\dots 15 = \dots 3 \cdot \left(\frac{1^3 + 1^2}{2} \right) + \dots 2 \cdot \left(\frac{2^3 + 2^2}{2} \right)$$

$$\dots 90 = \dots 6 \cdot \left(\frac{1^3 + 1^2}{2} \right) + \dots 5 \cdot \left(\frac{2^3 + 2^2}{2} \right) + \dots 3 \cdot \left(\frac{3^3 + 3^2}{2} \right)$$

$$\dots 350 = \dots 10 \cdot \left(\frac{1^3 + 1^2}{2} \right) + \dots 9 \cdot \left(\frac{2^3 + 2^2}{2} \right) + \dots 7 \cdot \left(\frac{3^3 + 3^2}{2} \right) + \dots 4 \cdot \left(\frac{4^3 + 4^2}{2} \right)$$

$$1050 = \dots 15 \cdot \left(\frac{1^3 + 1^2}{2} \right) + \dots 14 \cdot \left(\frac{2^3 + 2^2}{2} \right) + \dots 12 \cdot \left(\frac{3^3 + 3^2}{2} \right) + \dots 9 \cdot \left(\frac{4^3 + 4^2}{2} \right) + \dots 5 \cdot \left(\frac{5^3 + 5^2}{2} \right)$$

$$2646 = \dots 21 \cdot \left(\frac{1^3 + 1^2}{2} \right) + \dots 20 \cdot \left(\frac{2^3 + 2^2}{2} \right) + \dots 18 \cdot \left(\frac{3^3 + 3^2}{2} \right) + \dots 15 \cdot \left(\frac{4^3 + 4^2}{2} \right) + \dots 11 \cdot \left(\frac{5^3 + 5^2}{2} \right) + \dots 6 \cdot \left(\frac{6^3 + 6^2}{2} \right)$$

Set of the **parenthesis's coefficients** in up relations make a triangular array as below

"Figure 6"

Squared array No.3 created on the basis of row $n=3$ in Stirling squared array

"Figure 7"

Set of the **parenthesis's coefficients** in up relations make a triangular array as below

"Figure 6"

1							
3	2						
6		5	3				
10			7	4			
15				9	5		
21					6		
28						7	
36							8
35							
33							
30							
26							
21							
15							
11							
6							
13							
7							
15							
8							

By transferring the columns of above made triangular arrays, to top of arrays we will create **squared**

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1
3	1	1	1	1	1	1	1	1
4	1	1	1	1	1	1	1	1
5	1	1	1	1	1	1	1	1
6	1	1	1	1	1	1	1	1
7	1	1	1	1	1	1	1	1
8	1	1	1	1	1	1	1	1
9	1							

Squared array No.4 created on the basis of row $n=4$ in Stirling squared array

"Figure 8"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	2	3	4	5	6	7	8
2	3	5	7	9	11	13	15	17
3	6	9	12	15	18	21	24	27
4	10	14	18	22	26	30	34	38
5	15	20	25	30	35	40	45	50
6	21	27	33	39	45	51	57	63
7	28	35	42	49	56	63	70	77
8	36	44	52	60	68	76	84	92
9	45							

Squared array No.5 created on the basis of row $n=5$ in Stirling squared array

"Figure 9"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	4	9	16	25	36	49	64
2	7	19	37	61	91	127	169	217
3	25	55	97	151	217	295	385	487
4	65	125	205	305	425	565	725	905
5	140	245	380	545	740	965	1220	1505
6	266	434	644	896	1190	1526	1904	2324
7	462	714	1022	1386	1806	2282	2814	3402
8	750	1110	1542	2046	2622	3270	3990	4782
9	1155							

Squared array No.6 created on the basis of row $n=6$ in Stirling squared array

"Figure 10"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	8	27	64	125	216	343	512
2	15	65	175	369	671	1105	1695	2465
3	90	285	660	1275	2190	3465	5160	7335
4	350	910	1890	3410	5590	8550	12410	17290
5	1050	2380	4550	7770	12250	18200	25830	35350
6	2646	5418	9702	15834	24150	34986	48678	65562
7	5880	11130	18900	29694	44016	62370	85260	113190
8	11880	21120	34320	52200	75480	104880	141120	184920
9	22275							

Squared array No.7 created on the basis of row $n=7$ in Stirling squared array "need to be complete"

"Figure 11"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	16	81	256	625	1296	2401	4096
2	31	211	781	2101	4651	9031	15961	26281
3	301	1351	4081	9751	19981	36751	62401	
4	1701	5901	15421	33621	64701	113701		
5	6951	20181	47271	95781	174951			
6	22827	58107	124887	238287				
7	63987	147147	294987					
8	159027	337227						
9	359502							

Squared array No.8 created on the basis of row $n=8$ in Stirling squared array "need to be complete"

"Figure 12"

$n \setminus k$	1	2	3	4	5	6	7	8
1	1	32	243	1024	3125	7776	16807	32768
2	63	665	3367	11529	31031	70993	144495	
3	966	6069	23772	70035	170898	365001		
4	7770	35574	116298	305382	688506			
5	42525	156660	447195	1071630				
6	179487	563409	1446291					
7	627396	1740585						
8	1899612							
9								

Set of the above made squared arrays makes a three – dimensional "3D numerical array"

In the name **numerical cube array**

Important points:

In all of obtained squared arrays, the values which locate in first columns " $k = 1$ " are as same as the numbers which locate in a row of **squared Stirling array**

In all of obtained squared arrays, the values which locate in first rows " $n = 1$ " are the powers of first natural numbers.

The numbers are located in same **columns or rows or diagonals** on each one of the squared array, have relations with together and make progression series in different deeps.

For example progression series of numbers which locate in row " $n = 3$ " of squared array " $a = 5$ "
Is as below

25	55	97	151	217	295	385	487
30	42	54	66	78	90	102	
12	12	12	12	12	12	12	

By changing the number of "**n or k**" in squared arrays the **deep** of sequences will change

For example sequence of values locate in row $n=3$ of squared array $a=6$ is as below.

90	285	660	1275	2190	3465	5160	7335
195	375	615	915	1275	1695	2175	
180	240	300	360	420	480		
60	60	60	60	60	60		

Also each one of the squared array have relations with **previous** or **next** squared arrays by two below relations or formulas and the numbers of them make chain stitch **sequence** with together

$$\begin{pmatrix} a \\ n \\ k \end{pmatrix} = \begin{pmatrix} a \\ n-1 \\ k \end{pmatrix} + \begin{pmatrix} a-1 \\ n \\ k \end{pmatrix} \cdot (n+k-1)$$

$$\begin{pmatrix} a \\ n \\ k \end{pmatrix} = \begin{pmatrix} a \\ n-1 \\ k+1 \end{pmatrix} + \begin{pmatrix} a-1 \\ n \\ k \end{pmatrix} \cdot (k)$$

Example for relation 1

array $a=6$ row $n=7$ column $k=3$

$$\begin{pmatrix} 6 \\ 7 \\ 3 \end{pmatrix} = \begin{pmatrix} 6 \\ 7-1 \\ 3 \end{pmatrix} + \begin{pmatrix} 6-1 \\ 7 \\ 3 \end{pmatrix} \cdot (7+3-1)$$

$$(18900) = (9702) + (1022) \cdot (7+3-1)$$

Example for relation 2

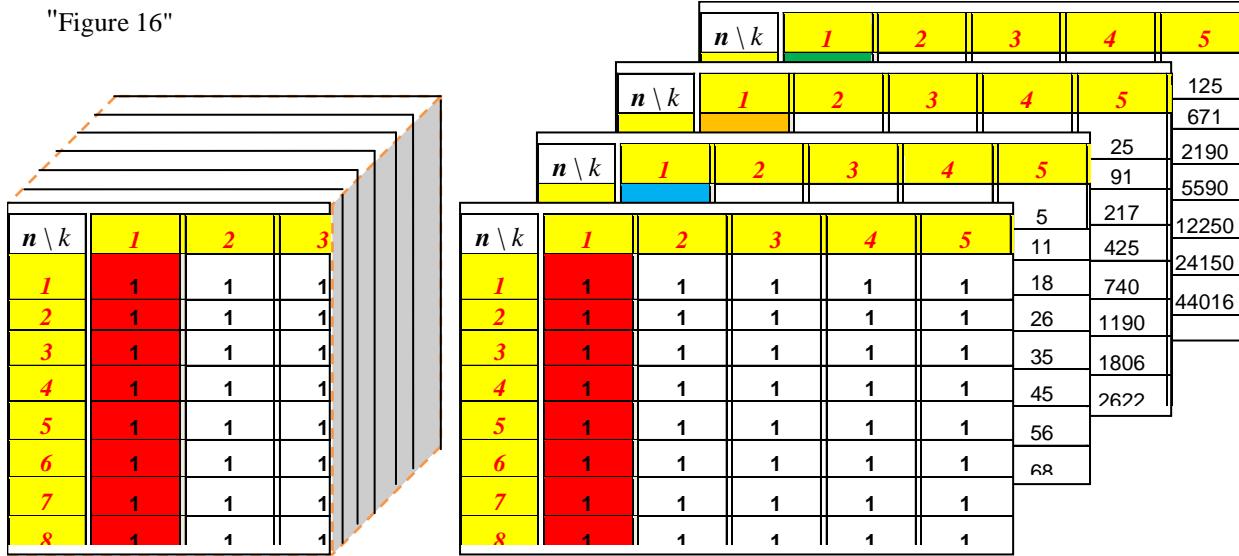
array $a=6$ row $n=7$ column $k=3$

$$\begin{pmatrix} 6 \\ 7 \\ 3+1 \end{pmatrix} = \begin{pmatrix} 6 \\ 7-1 \\ 3+1 \end{pmatrix} + \begin{pmatrix} 6-1 \\ 7 \\ 3 \end{pmatrix} \cdot (k)$$

$$(18900) = (1584) + (1022) \cdot (3)$$

Set of the above made squared arrays makes a three – dimensional "3D numerical array"
In the name **numerical cube array**

"Figure 16"



Numerical cube set of the squared arrays make three dimensional **numerical cube array**

By adding {3} to each one of base numbers, the 4th term of sequence will be obtain {42525 ,156660 ,447195 ,1071630 ,..}



Squared array No.6

row No {n = 6}

2646	5418	9702	15834	24150	34986
	2772		4284	6132	
		1512		1848	
			336	336	336

Squared array No.6

diagonal No.1

row No. {n = 1,2,3,4,..}

1	65	660	3410	12250	34986	85260	184920	366795
	64	595	2750	8840	22736	50274	99660	181875
	531	2155	6090	13896	27538	49386	82215	
	1624	3935	7806	13642	21848	32829		
	2311	3871	5836	8206	10981			
		1560	1965	2370	2775			
			405	405	405			

Squared array No.6

column No. {k = 1}

1	15	90	350	1050	2646	5880	11880
	14	75	260	700	1596	3234	6000
	61	185	440	896	1638	2766	
	124	255	456	742	1128		
		131	201	286	386		
			70	85	100		
				15	15		

Equations of packages {42525} for adding values {1,2,3,..N} instead of {A1} in Excel for getting the term of sequence

0	0 0
(1+A1)^5+(2+A1)^5+(3+A1)^5+(4+A1)^5+(5+A1)^5	4425
(2+3+4+5+4*A1)*(1+A1)^4*(1+3+4+5+4*A1)*(2+A1)^4*(1+2+4+5+4*A1)*(3+A1)^4*(1+2+3+5+4*A1)*(4+A1)^4*(1+2+3+4+4*A1)*(5+A1)^4	10260
(2+3+4+5+4*A1)*(1+A1)^3*(5+A1)+(1+3+4+5+4*A1)*(2+A1)^3*(5+A1)+(1+2+4+5+4*A1)*(3+A1)^3*(5+A1)+(1+2+3+5+4*A1)*(4+A1)^3*(5+A1)	5730
(2+3+4+3*A1)*(1+A1)^3*(4+A1)+(1+3+4+3*A1)*(2+A1)^3*(4+A1)+(1+2+4+3*A1)*(3+A1)^3*(4+A1)	1048
(2+3+2*A1)*(1+A1)^3*(3+A1)+(1+3+2*A1)*(2+A1)^3*(3+A1)	111
(2+A1)*(1+A1)^3*(2+A1)	4
(2+3+4+5+4*A1)*(1+A1)^2*(5+A1)+(1+3+4+5+4*A1)*(2+A1)^2*(5+A1)+(1+2+4+5+4*A1)*(3+A1)^2*(5+A1)+(1+2+3+5+4*A1)*(4+A1)^2*(5+A1)	8750
(2+3+4+3*A1)*(1+A1)^2*(4+A1)*(5+A1)+(1+3+4+3*A1)*(2+A1)^2*(4+A1)*(5+A1)+(1+2+4+3*A1)*(3+A1)^2*(4+A1)*(5+A1)	2080
(2+3+2*A1)*(1+A1)^2*(3+A1)*(5+A1)+(1+3+2*A1)*(2+A1)^2*(3+A1)*(5+A1)	315
(2+A1)*(1+A1)^2*(2+A1)*(5+A1)	20
(2+3+4+3*A1)*(1+A1)^2*(4+A1)*(4+A1)+(1+3+4+3*A1)*(2+A1)^2*(4+A1)*(4+A1)+(1+2+4+3*A1)*(3+A1)^2*(4+A1)*(4+A1)	1664
(2+3+2*A1)*(1+A1)^2*(3+A1)*(4+A1)+(1+3+2*A1)*(2+A1)^2*(3+A1)*(4+A1)	252
(2+A1)*(1+A1)^2*(2+A1)*(4+A1)	16
(2+3+2*A1)*(1+A1)^2*(3+A1)*(3+A1)+(1+3+2*A1)*(2+A1)^2*(3+A1)*(3+A1)	189
(2+A1)*(1+A1)^2*(2+A1)*(3+A1)	12
(2+A1)*(1+A1)^2*(2*(2+A1)*(2+A1))	8
(1+A1)*(2+A1)*(5+A1)*(5+A1)+(1+2+2*A1)*(3+A1)*(5+A1)*(5+A1)	4375
(1+A1)*(2+A1)*(4+A1)*(4+A1)*(5+A1)+(1+2+2*A1)*(3+A1)*(4+A1)*(4+A1)*(5+A1)	880
(1+A1)*(2+A1)*(3+A1)*(3+A1)*(5+A1)	90
(1+A1)*(2+A1)*(4+A1)*(5+A1)*(5+A1)+(1+2+2*A1)*(3+A1)*(4+A1)*(5+A1)*(5+A1)	1100
(1+A1)*(2+A1)*(3+A1)*(4+A1)*(5+A1)	120
(1+A1)*(2+A1)*(3+A1)*(5+A1)*(5+A1)	150
(1+A1)*(2+A1)*(4+A1)*(4+A1)*(4+A1)+(1+2+2*A1)*(3+A1)*(4+A1)*(4+A1)*(4+A1)	704
(1+A1)*(2+A1)*(3+A1)*(3+A1)*(4+A1)	72
(1+A1)*(2+A1)*(3+A1)*(4+A1)*(4+A1)	96
(1+A1)*(2+A1)*(3+A1)*(3+A1)*(3+A1)	54
42525	42525